

Two-Sample Z Test for Proportions

Verified Python analysis transcript

Test: Two-Sample Z Test for Proportions

Design: Asymptotic comparison of male and female G3 pass proportions.

Variables: sex, G3 >= 10

Null hypothesis: The two population pass proportions are equal.

Primary formula: $z = (p_1 - p_2) / \sqrt{p_{\text{pool}}(1 - p_{\text{pool}})(1/n_1 + 1/n_2)}$

Valid source rows: 649

Verified results:

z_statistic: -1.9927454994231857

p_value: 0.04628932237899876

male_proportion: 0.8120300751879699

female_proportion: 0.8694516971279374

difference: -0.05742162193996747

pooled_standard_error: 0.028815331389075306

unpooled_standard_error: 0.02949886508675137

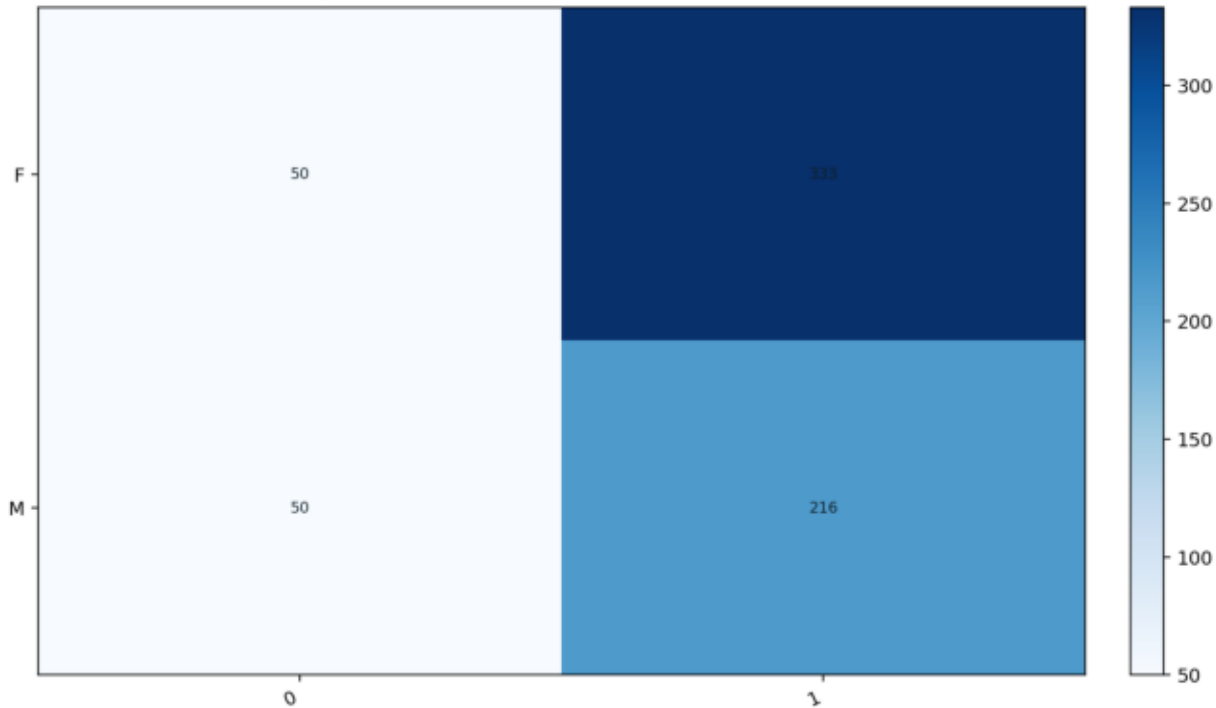
Interpretation:

$z = -1.992745$, $p = 0.0462893$; male-female proportion difference = -0.057422.

The null test uses the pooled standard error; confidence intervals use unpooled group uncertainty.

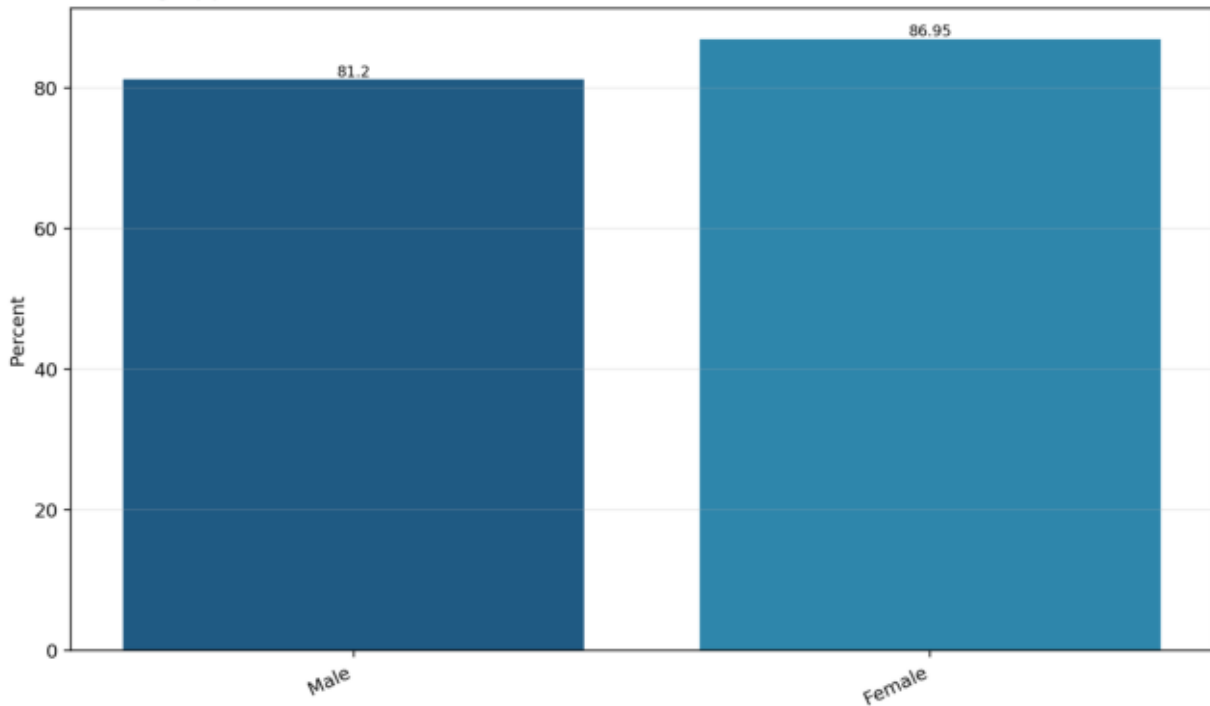
Sex and G3 pass outcome

Observed counts for the two-sample z test



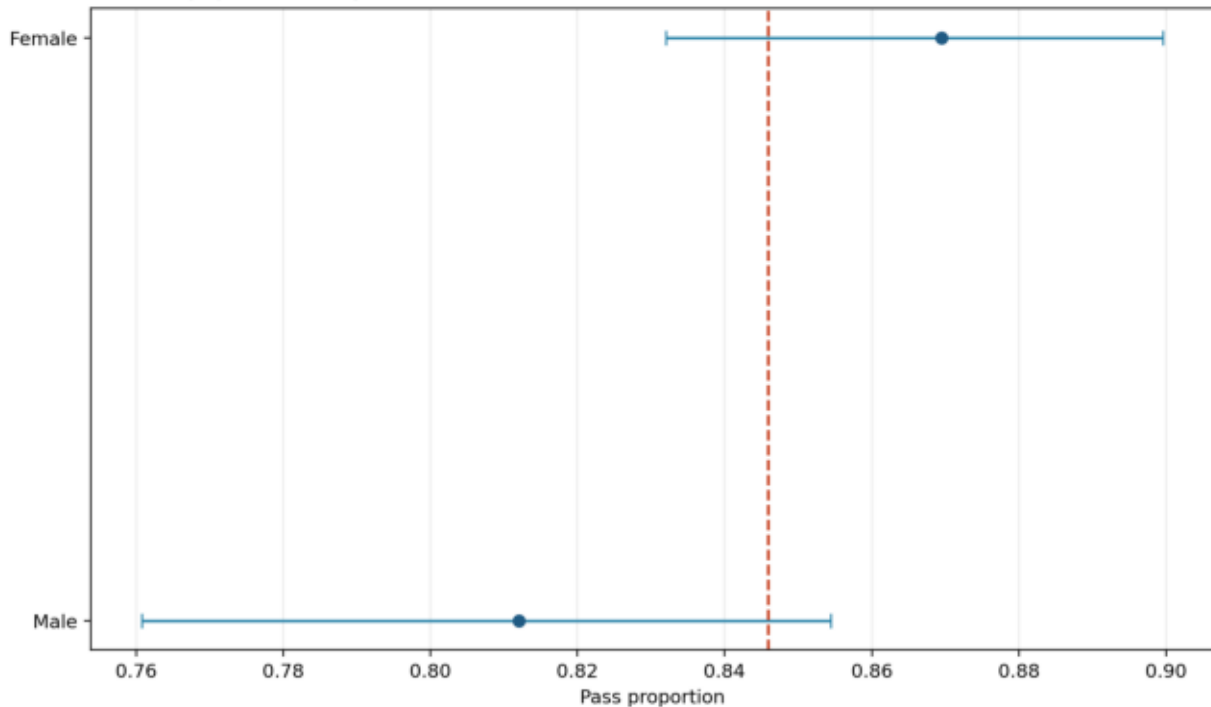
Pass proportions by sex

Observed group probabilities



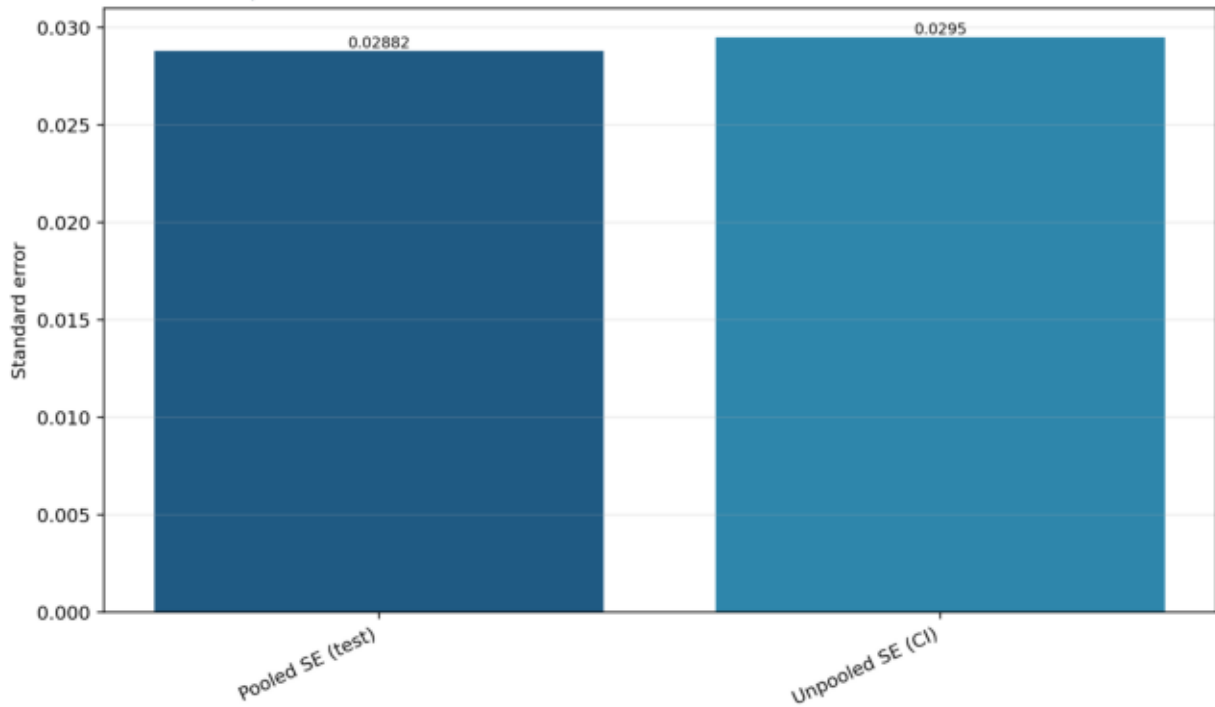
Group proportions with Wilson intervals

Pooled null proportion shown by the red line



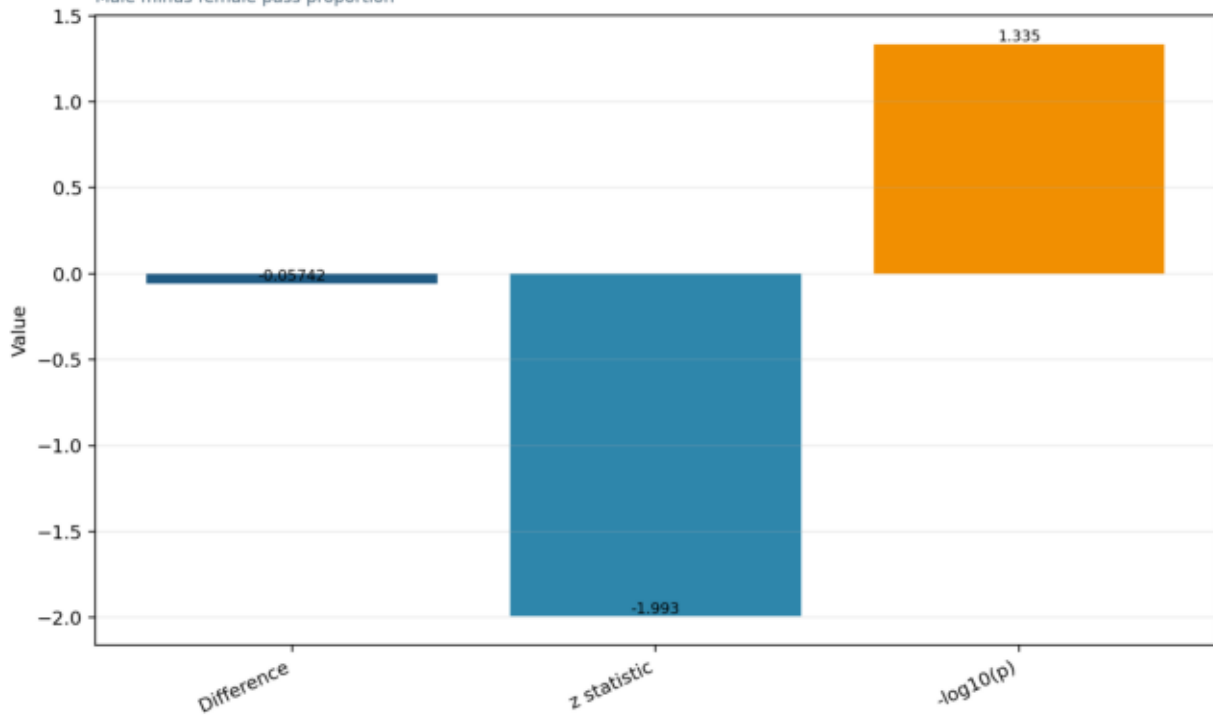
Standard-error roles

Pooled for H_0 ; unpooled for the difference interval



Two-proportion z-test result

Male minus female pass proportion



Observed 2X2

0	1
50	333
50	216

Group Proportions

successes	n	proportion	ci_low	ci_high
216	266	0.81203	0.760762	0.854414
333	383	0.869452	0.83201	0.899556